

$$1. \text{ Average Speed} = \frac{\Delta y}{\Delta t} = \frac{16(3)^2 - 16(0)^2}{3 - 0} = \frac{144}{3} \frac{\text{ft}}{\text{sec}} = 48 \frac{\text{ft}}{\text{sec}}$$

$$3. \text{ Average speed} = \frac{\Delta y}{\Delta t} = \frac{16(3+h)^2 - 16(3)^2}{h}$$

$$\frac{\Delta y}{\Delta t} = \frac{16(9+6h+h^2) - 16 \cdot 9}{h} = \frac{144 + 96h + 16h^2 - 144}{h} = \frac{96h + 16h^2}{h}$$

$$\frac{\Delta y}{\Delta t} = 96 + 16h$$

$$\text{Instantaneous speed} = \lim_{h \rightarrow 0} (96 + 16h) = 96 \frac{\text{ft}}{\text{sec}}$$

$$5. \lim_{x \rightarrow c} (2x^3 - 3x^2 + x - 1) = 2c^3 - 3c^2 + c - 1$$

$$9. \lim_{x \rightarrow 1} (x^3 + 3x^2 - 2x - 17) = (1)^3 + 3(1)^2 - 2(1) - 17 = 1 + 3 - 2 - 17 = -15$$

$$15. f(x) = \frac{x^2 + 6x + 2}{x + 1} \quad a. \begin{array}{c|c|c|c|c} x & -0.1 & -0.01 & -0.001 & -0.0001 \\ \hline f(x) & 1.567 & 1.960 & 1.996 & 2.0 \end{array}$$

$$b. \begin{array}{c|c|c|c|c} x & 0.1 & 0.01 & 0.001 & 0.0001 \\ \hline f(x) & 2.373 & 2.040 & 2.004 & 2.0004 \end{array} \quad \lim_{x \rightarrow 0} f(x) = 2$$

$$23. \lim_{x \rightarrow 0} \frac{|x|}{x} \quad \text{you cannot substitute zero into the } x\text{'s because you would cause division by zero, which results in an undefined value.}$$

$$\lim_{x \rightarrow 0^-} \frac{|x|}{x} = -1 \quad \lim_{x \rightarrow 0^+} \frac{|x|}{x} = 1 \quad \text{since } \lim_{x \rightarrow 0^-} f(x) \neq \lim_{x \rightarrow 0^+} f(x),$$

the limit of the function as x approaches 0 DNE.

$$25. \lim_{x \rightarrow 1} \frac{x-1}{x^2-1} = \frac{1}{2} \quad \text{Try this: } \lim_{x \rightarrow 1} \frac{x-1}{(x-1)(x+1)} = \lim_{x \rightarrow 1} \frac{1}{x+1} = \frac{1}{2}$$